## Function Summary 14 July 2020

Go through the following summary of functions
Linear functions of the form $y=m x+c$.

| Domain | X E R |
| :--- | :--- |
| Range | Y E R |
| $\boldsymbol{m}$ changes (Gradient Changes) | The Slope changes. |
| $\boldsymbol{c}$ changes ( $y$-intercept Changes) | The graph cuts the $y$ axis at $q$. <br> The graph can shift up or down then in <br> comparison with original graph. <br> Example $f(x)=x-2$ |
| $g(x)=x-5$ |  |
| The graph of $g(x)$ cuts the $y$-axis at -5. |  |
| Therefore $g(x)$ has moved down 3 units from $f(x)$ |  |
| graph. |  |

Quadratic functions of the form $y=a x^{2}+q$.

| Domain | X E R |
| :--- | :--- |
| Range | If $\boldsymbol{a}$ is positive <br> $\mathrm{Y} \geq \mathrm{q}$ <br> If $\boldsymbol{a}$ is negative <br> $\mathrm{Y} \leq \mathrm{q}$ |
| a change | If $\mathrm{a} \geq 0$ |
| $\boldsymbol{q}$ changes |  |

Hyperbolic functions of the form $y=\frac{a}{x}+q$.

| Domain | XE R; $x \neq 0$ |
| :--- | :--- |
| Range | YE R; $y \neq q$ |
| a change | The value of $y$ at $x=1$ will be a <br> The value of $y$ at $x=-1$ will be a <br> ALSO REMEMBER <br> If $a>0$ |
|  |  |
|  |  |

q changes

Exponential functions of the form $y=a b^{x}+q$.


SUMMARY FOR ALL GRAPH SHIFTS

| Function change | Shift |
| :--- | :--- |
| $f(x)+c$ | Shift the graph of $f(x)$ up $c$ units |
| $f(x)-c$ | Shift the graph of $f(x)$ down $c$ units |
| $f(x+c)$ | Shift the graph of $f(x)$ left $c$ units |
| $f(x-c)$ | Shift the graph of $f(x)$ right $c$ units |
|  |  |
| $-f(x)$ | Reflect the graph of $f(x)$ about the $x-a x i s$ |
| $f(-x)$ | Reflect the graph of $f(x)$ about the $y$-axis |
|  |  |
| $f(c . x)$ | Compress the graph of $f(x)$ horizontally by a factor of $c$. |
| $c . f(x)$ | Stretch the graph of $f(x)$ vertically by a factor of $c$. |

## Textbook Exercises

## Page 84 Exercise 1 number 1 (I put them on separate axes each time so you can see the graphs)


1.2

$1.3 g(x)=-1 / 2 x^{2}+2$

$1.5 h(x)=1 / 2 x^{2}$
1.6

$1.7 \mathrm{k}(\mathrm{x})=1 / 2 \mathrm{x}^{2}-2$
VERTICAL SHIFTS
Page 84 Exercise 1 number 2 (Try yourself)

## Page 85 Exercise 2

## Example for Number 1

1. $\mathrm{y}=\mathrm{x}^{2}+6 \mathrm{x}+9$

## FACTORISE

$y=(x+3)^{2}$
Therefore, the shift from the origin is 3 units left.

## ILLUSTRATED AS GRAPHS



## HORIZONTAL AND VERTICAL SHIFTS

Standard Form to make it easier is $y=(x+p)^{2}+q$
Where $p$ is the horizontal shift
Where $q$ is the vertical shift
How would you change $y=x^{2}+4 x+12$ into $y=(x+p)^{2}+q$ form
COMPLETE THE SQUARE METHOD - you just not solving for $x$
$y=\left(x^{2}+4 x+4\right)+12-4$
$y=(x+2)^{2}+8$

$$
\left(\frac{\text { Coefficient of } b}{2}\right)^{2}\left(\frac{4}{2}\right)^{2}=2^{2}
$$

ADD and SUBTRACT TO NOT CHANGE THE EXPRESSION

There the shift from origin is 2 units to the left and 8 units up.


## Page 86 Exercise 3 (ALREADY IN THE STANDARD FORM OF $y=(x+p)^{2}+q$

$$
\text { 1. } \begin{aligned}
& \text { X-INTERCEPT FORM } \\
& y=(x-4)^{2}-9 \\
& y=(x-4)(x-4)-9 \\
& y=x^{2}-8 x+16-9 \\
& y=x^{2}-8 x+7 \\
& y=(x-7)(x-1)
\end{aligned}
$$

## SHIFT

$y=(x-4)^{2}-9$
Shift 4 units to the right and 9 units down

## Page 86 Exercise 2 (Try yourself)

2 to 4

| Function change | Shift |
| :--- | :--- |
| $f(x)+c$ | Shift the graph of $f(x)$ up $c$ units |
| $f(x)-c$ | Shift the graph of $f(x)$ down $c$ units |
| $f(x+c)$ | Shift the graph of $f(x)$ left $c$ units |
| $f(x-c)$ | Shift the graph of $f(x)$ right $c$ units |
|  | Reflect the graph of $f(x)$ about the $x$-axis |
| $-f(x)$ | Reflect the graph of $f(x)$ about the $y$-axis |
| $f(-x)$ | Compress the graph of $f(x)$ horizontally by a <br> factor of $c$. |
| $f(c . x)$ | Stretch the graph of $f(x)$ vertically by a factor of <br> c. |
| $c . f(x)$ |  |

