

Question asked by a learner

9 June 2020

DOUBLE ANGLE QUESTION

$$\tan x = \frac{1 - \cos 2x}{\sin 2x}$$

RHS

$$\frac{1 - (\cos^2 x - \sin^2 x)}{\sin 2x}$$

$$\frac{1 - (\cos^2 x - \sin^2 x)}{2 \sin x \cdot \cos x}$$

$$\frac{1 - \cos^2 x + \sin^2 x}{2 \sin x \cdot \cos x}$$

$$\frac{\sin^2 x + \sin^2 x}{2 \sin x \cdot \cos x}$$

$$\frac{2 \sin^2 x}{2 \sin x \cdot \cos x}$$

$$\frac{\sin x}{\cos x}$$

$$= \tan x$$

$$\therefore LHS = RHS$$

$$\cos 2x = \cos^2 x - \sin^2 x$$

$$\cos 2x = 2 \cos^2 x - 1$$

$$\cos 2x = 1 - 2 \sin^2 x$$

$$\sin 2x = 2 \sin x \cdot \cos x$$

$$1 = \cos^2 x + \sin^2 x$$

$$1 - \cos^2 x = \sin^2 x$$

$$1 + \sin^2 x = \cos^2 x$$