

Gr 12

Average Gradient Example

Example 3

Give that: $f(x) = x^3 - 2x^2 - 7x - 4$

Determine the average gradient between $x = 0$ and $x = -1,5$

Answer

$$f(0) = -4$$

$$f(-1,5) = -1,375$$

$$\begin{aligned}\text{Average gradient} &= \frac{f(-1,5) - f(0)}{-1,5 - 0} \checkmark \checkmark \\ &= -1,75 \checkmark\end{aligned}$$

Example 4

Consider $f(x) = x^2 + 7x + 10$. Determine the average gradient between the points $x=2$ and $x=-1$

Answer

1. First work out the y value at $x=2$ and $x=-1$

LET $x_1=2$ and $x_2=-1$

$$f(2) = (2)^2 + 7(2) + 10.$$

$$f(2) = 4 + 14 + 10$$

$$f(2) = 28 = y_1$$

$$f(-1) = (-1)^2 + 7(-1) + 10$$

$$f(-1) = 1 - 7 + 10$$

$$f(-1) = 4 = y_2$$

2. Use the gradient formula

$$m = \frac{y_2 - y_1}{x_2 - x_1}$$

$$m = \frac{4 - 28}{-1 - 2}$$

$$m = \frac{-24}{-3} = 8$$

The average gradient between $x=2$ and $x=-1$ for $f(x)$ is 8.