



Topic 13

GEOMETRY OF 2D SHAPES SLIDES



Topic 13

GEOMETRY OF 2D SHAPES VIDEO 1

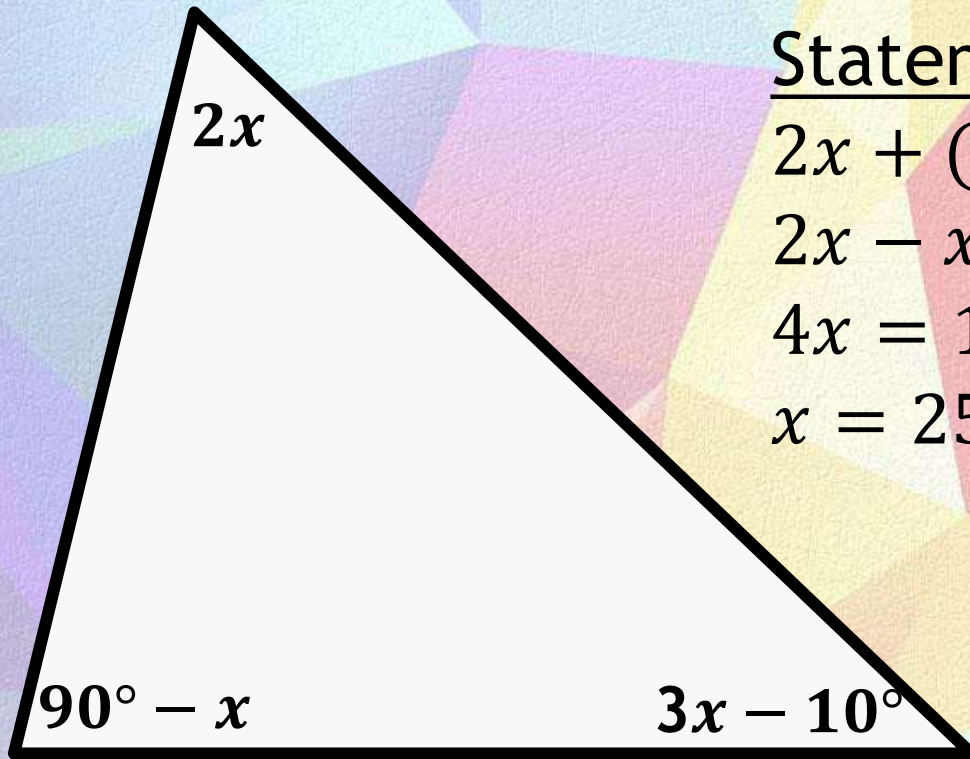


TRIANGLES

(3 REASONS)

∠s in a Δ

Angles of a Δ add up to 180°.



Statement

$$2x + (90^\circ - x) + (3x - 10^\circ) = 180^\circ$$

$$2x - x + 3x = 180^\circ - 90^\circ + 10^\circ$$

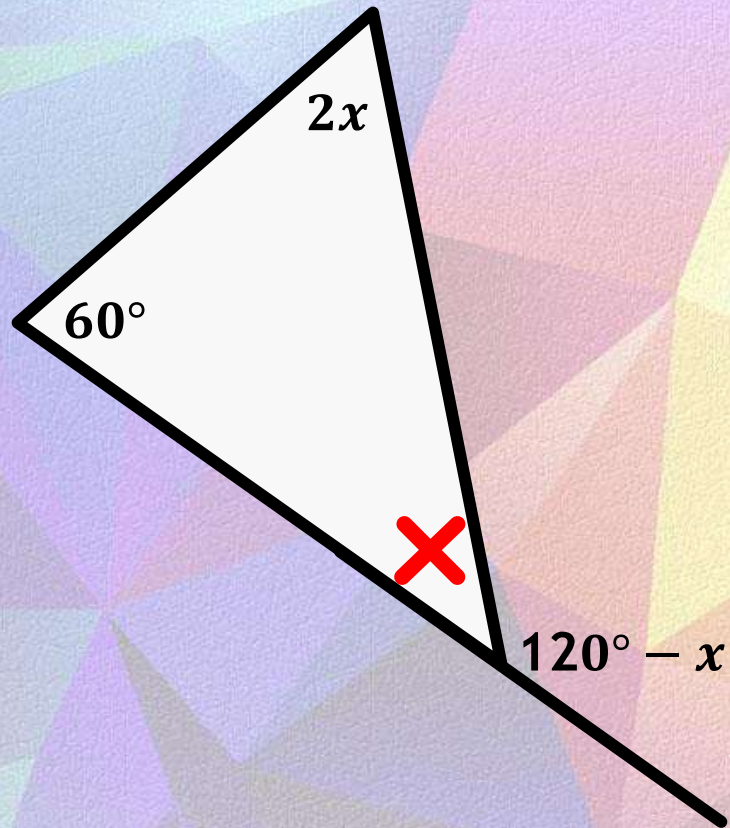
$$4x = 100^\circ$$

$$x = 25^\circ$$

Reason

∠s in a Δ

Ext \angle of Δ



The exterior angle of a triangle is equal to the **SUM OF THE OPPOSITE INTERIOR ANGLES**.

Statement

$$2x + 60^\circ = 120^\circ - x$$

$$2x + x = 120^\circ - 60^\circ$$

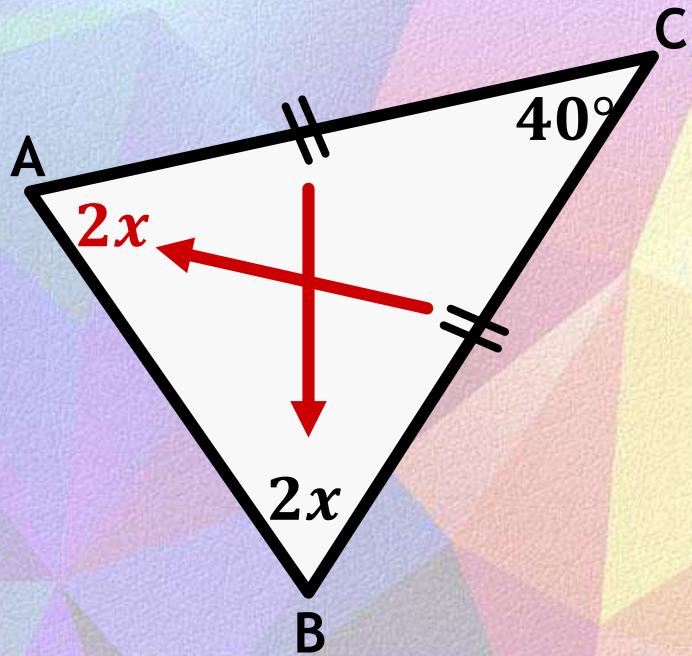
$$3x = 60^\circ$$

$$x = 20^\circ$$

Reason

Ext \angle of Δ

\angle opp = sides



Statement

$$\hat{A} = \hat{B} = 2x$$

$$2x + 2x + 40^\circ = 180^\circ$$

$$4x = 180^\circ - 40^\circ$$

$$4x = 140^\circ$$

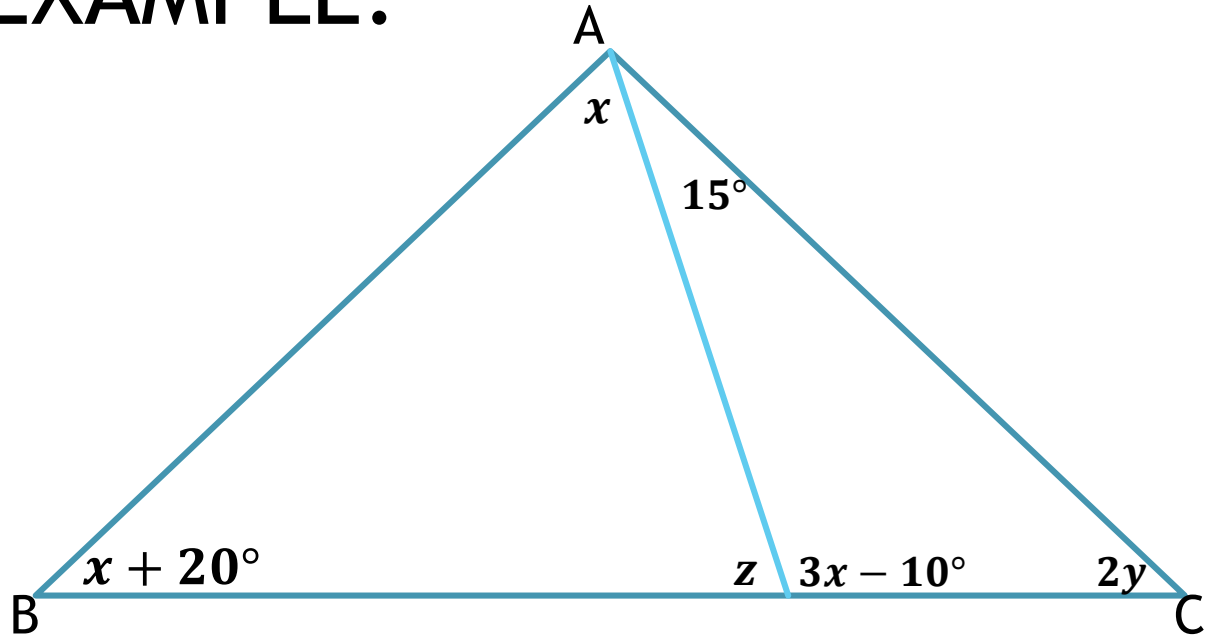
$$x = 35^\circ$$

Reason

\angle opp = sides

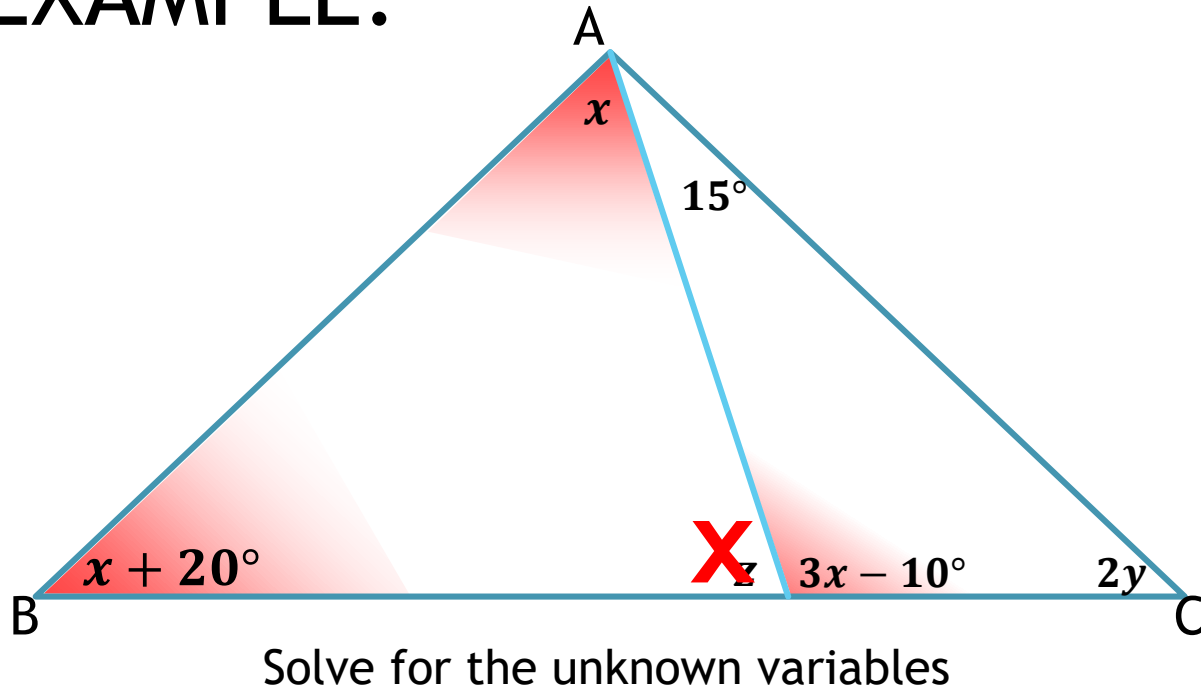
\angle in a Δ

EXAMPLE:



Solve for the unknown variables

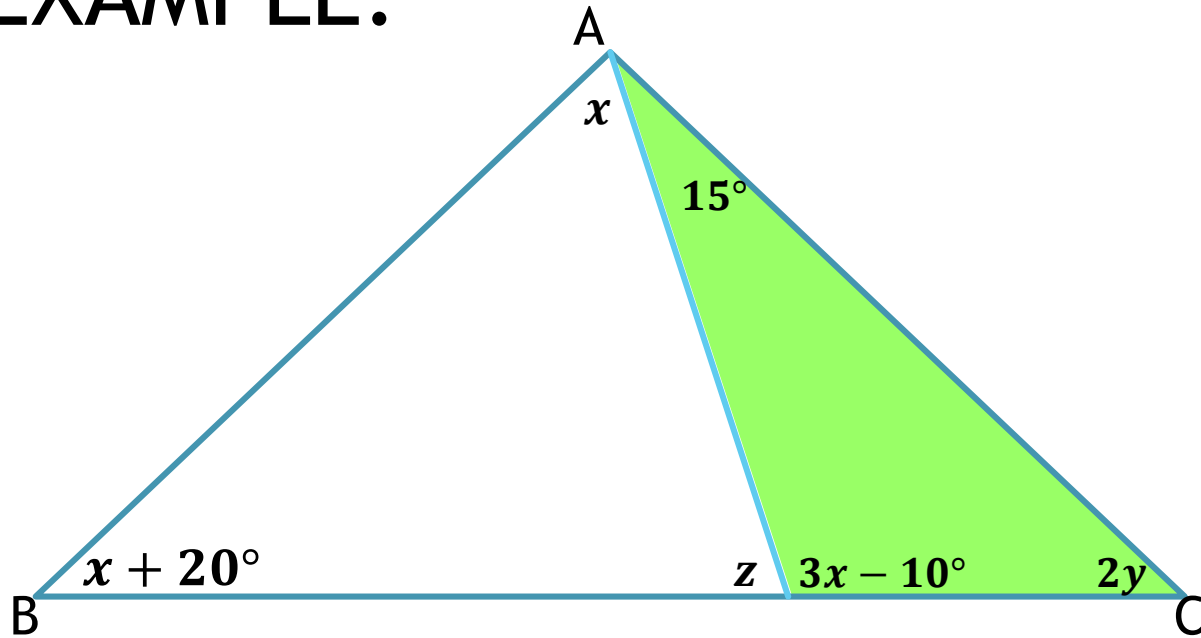
EXAMPLE:



Solve for x

| <u>Statement</u> | <u>Reason</u> |
|--|---|
| $(x + 20^\circ) + x = (3x - 10^\circ)$ | <i>Ext \angle of Δ</i> |
| $x + 20^\circ + x = 3x - 10^\circ$ | |
| $x + x - 3x = -10^\circ - 20^\circ$ | |
| $-x = -30^\circ$ | |
| $x = 30^\circ$ | |

EXAMPLE:



Solve for the unknown variables

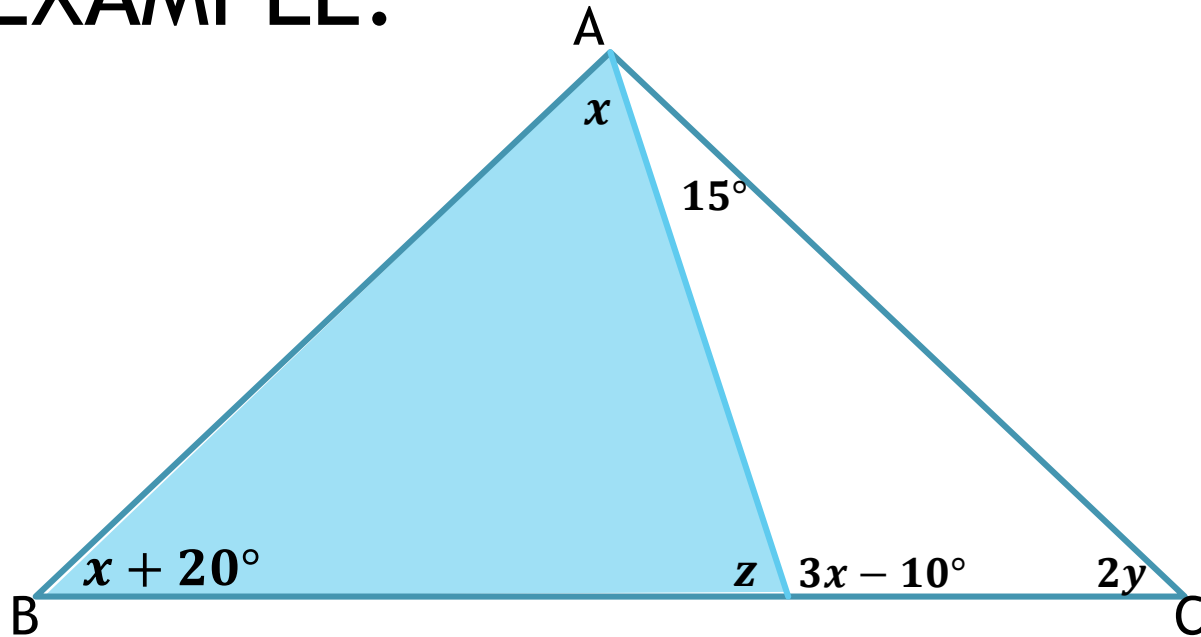
Solve for y

| Statement | Reason |
|--|---------------------------|
| $15^\circ + (3x - 10^\circ) + 2y = 180^\circ$ | \angle 's in a Δ |
| $15^\circ + 3(30^\circ) - 10^\circ + 2y = 180^\circ$ | |
| $15^\circ + 90^\circ - 10^\circ + 2y = 180^\circ$ | |
| $95 + 2y = 180$ | |
| $2y = 180 - 95$ | |
| $2y = 85$ | |
| $y = 42,5$ | |

Solve for x

| Statement | Reason |
|--|--------------------------|
| $(x + 20^\circ) + x = (3x - 10^\circ)$ | $Ext \angle$ of Δ |
| $x + 20^\circ + x = 3x - 10^\circ$ | |
| $x + x - 3x = -10^\circ - 20^\circ$ | |
| $-x = -30^\circ$ | |
| $x = 30^\circ$ | |

EXAMPLE:



Solve for the unknown variables

Solve for x

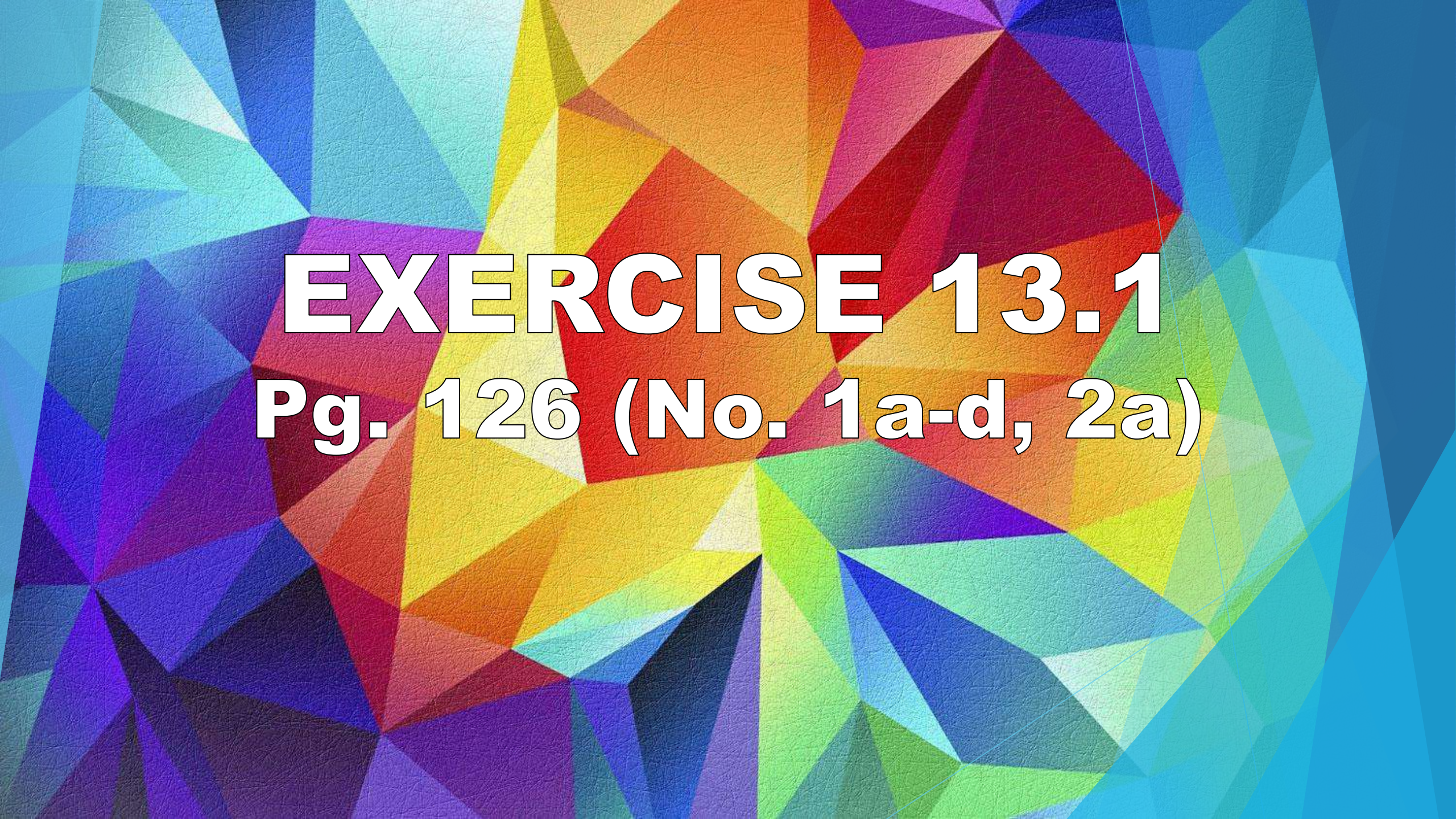
| Statement | Reason |
|--|---|
| $(x + 20^\circ) + x = (3x - 10^\circ)$ | <i>Ext \angle of Δ</i> |
| $x + 20^\circ + x = 3x - 10^\circ$ | |
| $x + x - 3x = -10^\circ - 20^\circ$ | |
| $-x = -30^\circ$ | |
| $x = 30^\circ$ | |

Solve for y

| Statement | Reason |
|--|---|
| $15^\circ + (3x - 10^\circ) + 2y = 180^\circ$ | <i>\angle's in a Δ</i> |
| $15^\circ + 3(30^\circ) - 10^\circ + 2y = 180^\circ$ | |
| $15^\circ + 90^\circ - 10^\circ + 2y = 180^\circ$ | |
| $95 + 2y = 180$ | |
| $2y = 180 - 95$ | |
| $2y = 85$ | |
| $y = 42,5$ | |

Solve for z

| Statement | Reason |
|--|---|
| $x + 20^\circ + x + z = 180^\circ$ | <i>\angle's in a Δ</i> |
| $(30^\circ) + 20^\circ + (30^\circ) + z = 180^\circ$ | |
| $80^\circ + z = 180^\circ$ | |
| $z = 180^\circ - 80^\circ$ | |
| $z = 100^\circ$ | |

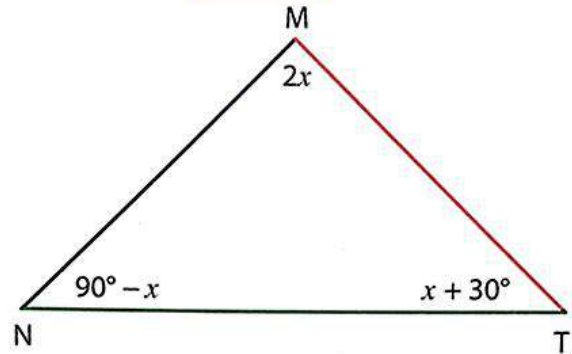


EXERCISE 13.1
Pg. 126 (No. 1a-d, 2a)

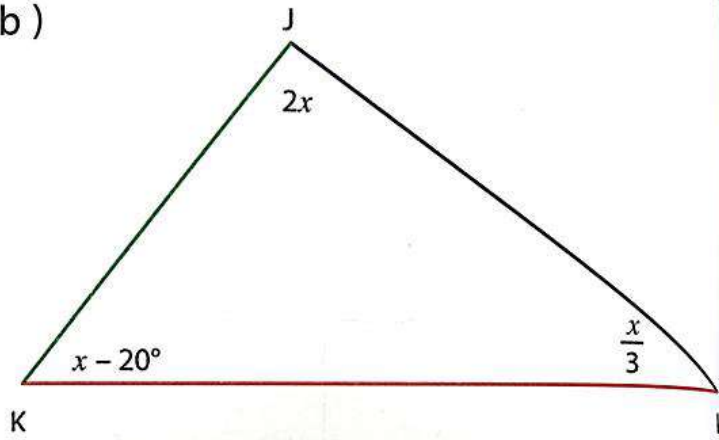
EXERCISE 13.1 Pg. 126 (No. 1a-d, 2a)

1. Solve for x and **classify** each triangle.

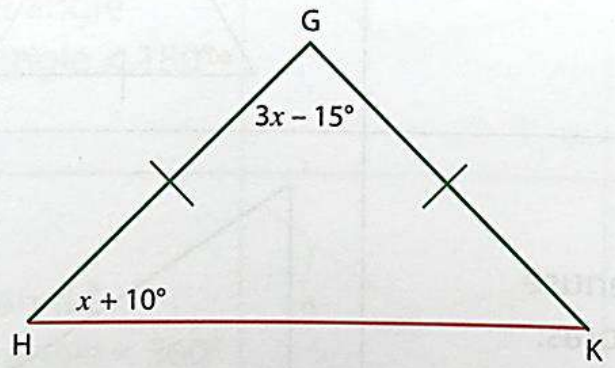
a)



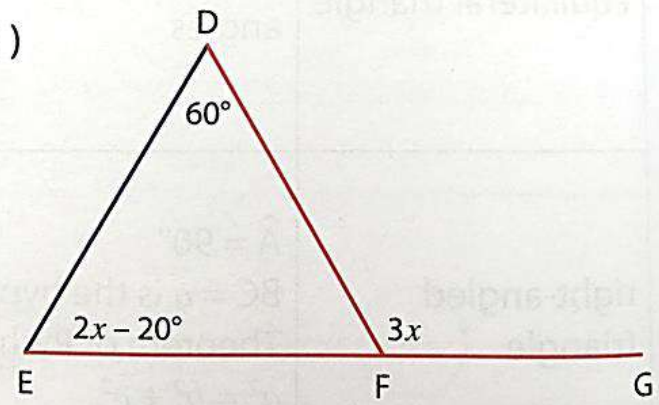
b)



c)

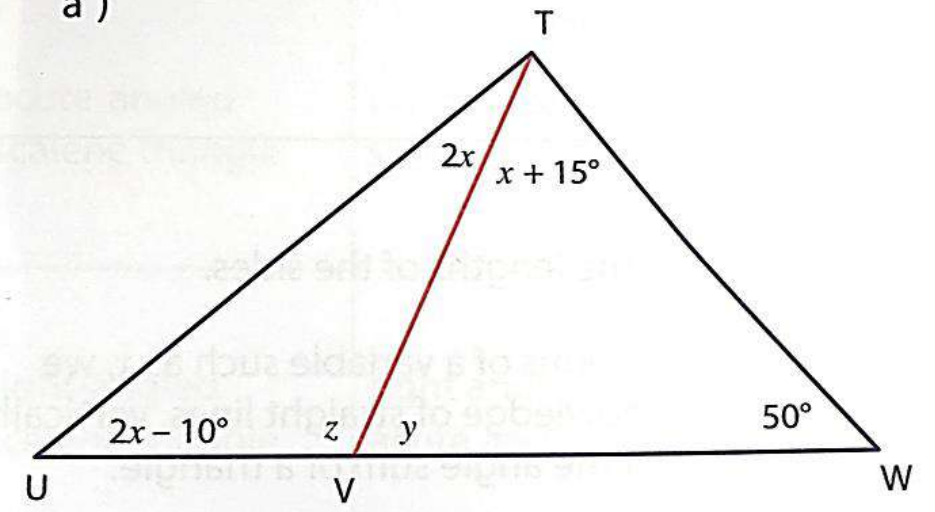


d)



2. Solve for x , y and z and **classify**, with reasons, the triangle.

a)





Topic 13

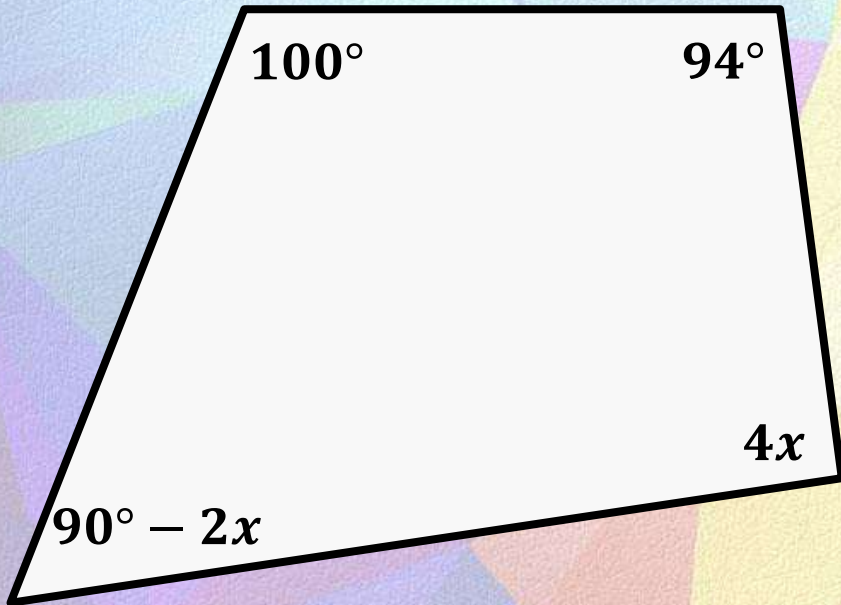
GEOMETRY OF 2D SHAPES VIDEO 2



QUADRILATERALS

(1 REASON)

∠s of a quad



Angles of a *quad* add up to **360°** .

Statement

Reason

$$100^\circ + (90^\circ - 2x) + 4x + 94^\circ = 360^\circ$$

∠s of a quad

$$100^\circ + 90^\circ - 2x + 4x + 94^\circ = 360^\circ$$

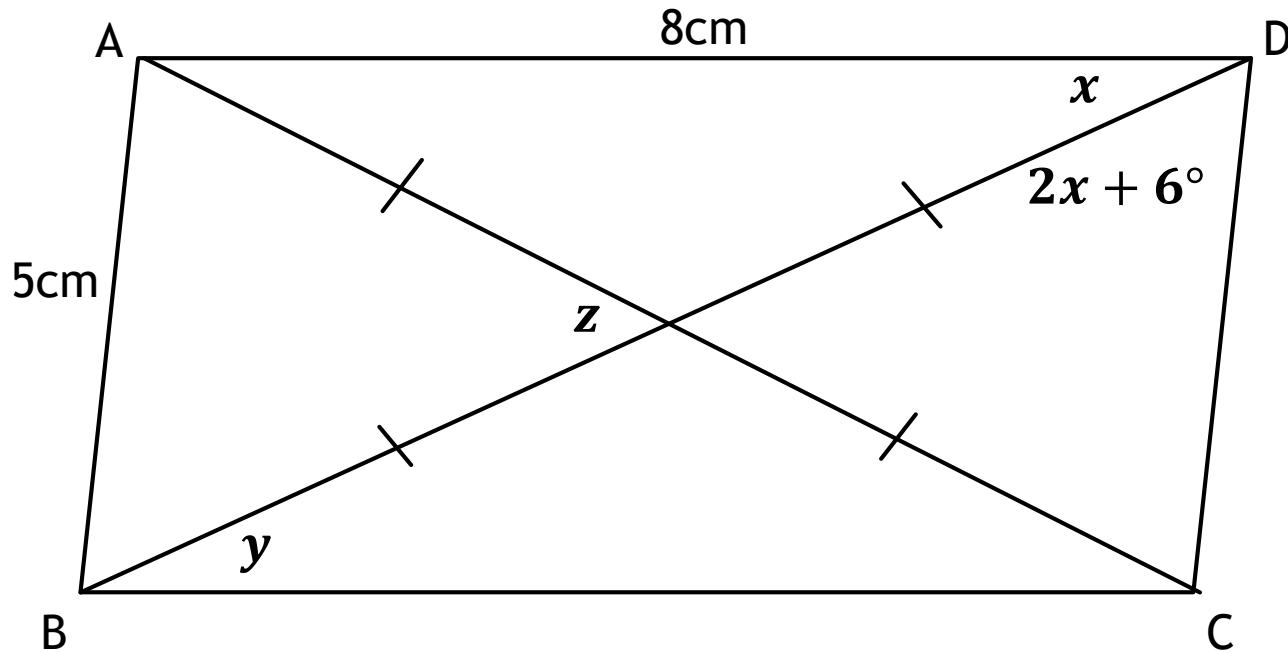
$$284^\circ + 2x = 360^\circ$$

$$2x = 360^\circ - 284^\circ$$

$$2x = 76^\circ$$

$$x = 38^\circ$$

EXAMPLE:



- 1.) Classify the quadrilateral ABCD, giving reasons for you answer.

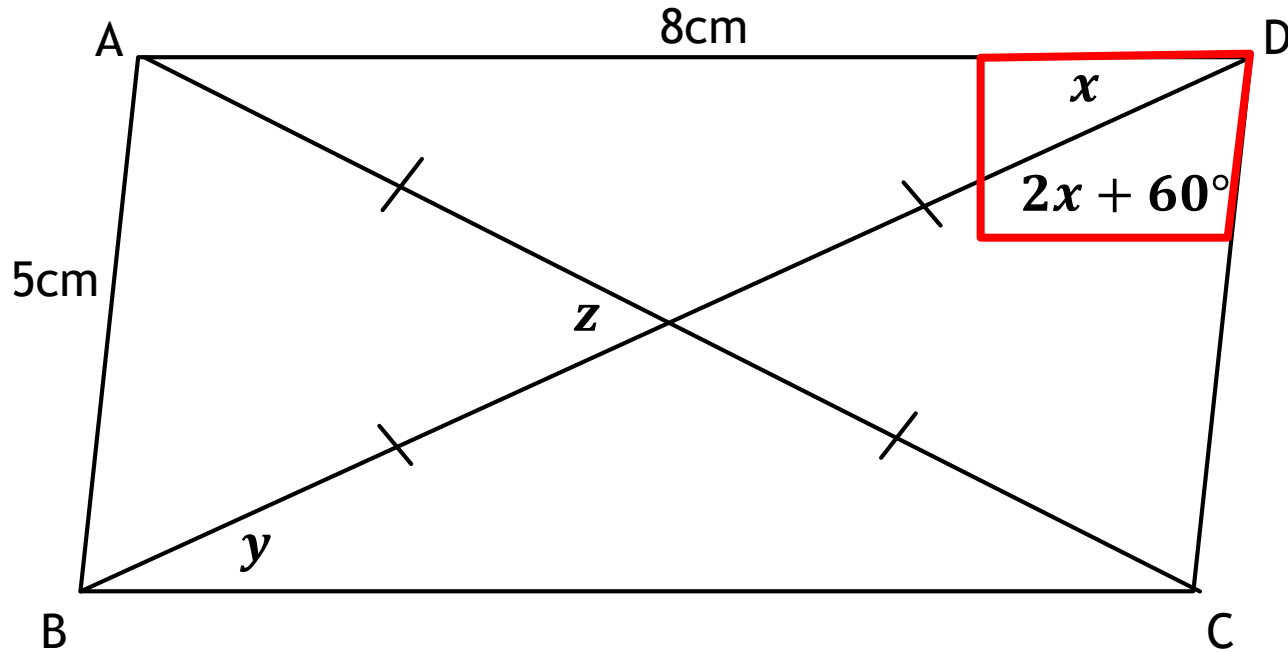
Diagonals are equal (*Square or Rectangle*)

Opposite sides are equal

\therefore It must be a rectangle

- 2.) Determine giving reasons x, y and z

EXAMPLE:



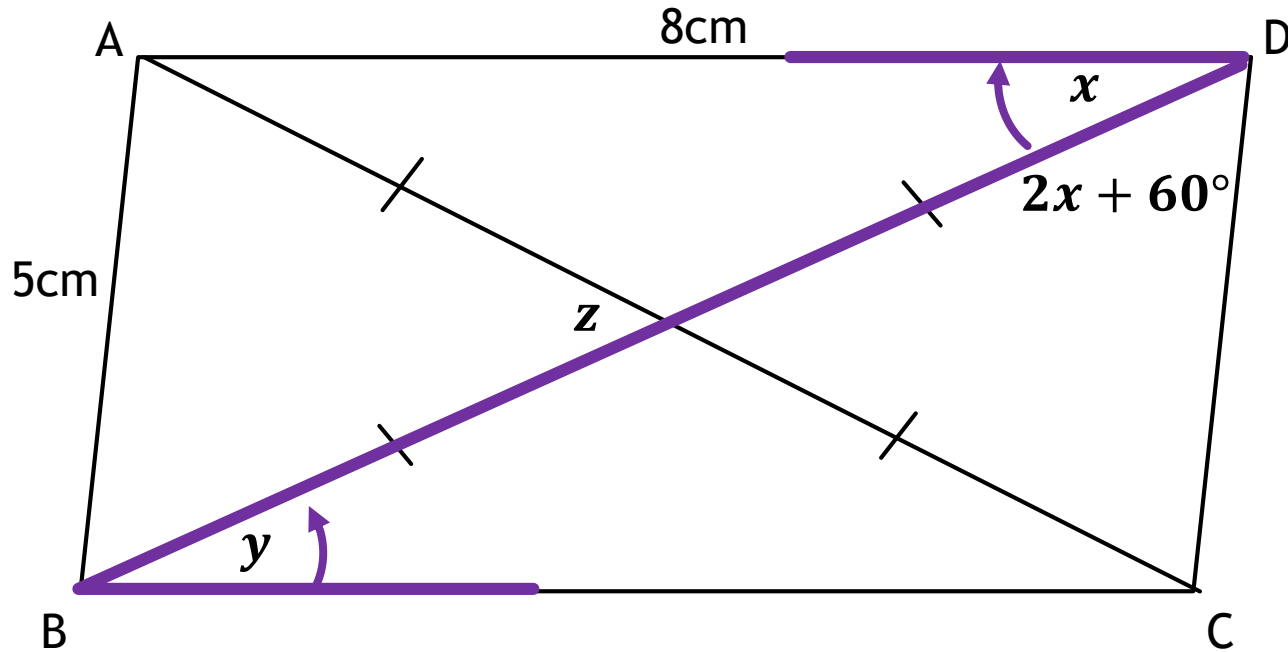
- 1.) Classify the quadrilateral ABCD, giving reasons for you answer.

Diagonals are equal (*Square or Rectangle*)
Opposite sides are equal
 \therefore It must be a rectangle

- 2.) Determine giving reasons x , y and z

$$\begin{aligned}x + 2x + 60^\circ &= 90^\circ && \text{Adj Comp } \angle\text{'s or} \\3x &= 90^\circ - 60^\circ && \text{Properties of a rect} \\3x &= 30^\circ \\x &= 10^\circ\end{aligned}$$

EXAMPLE:



- 1.) Classify the quadrilateral ABCD, giving reasons for your answer.

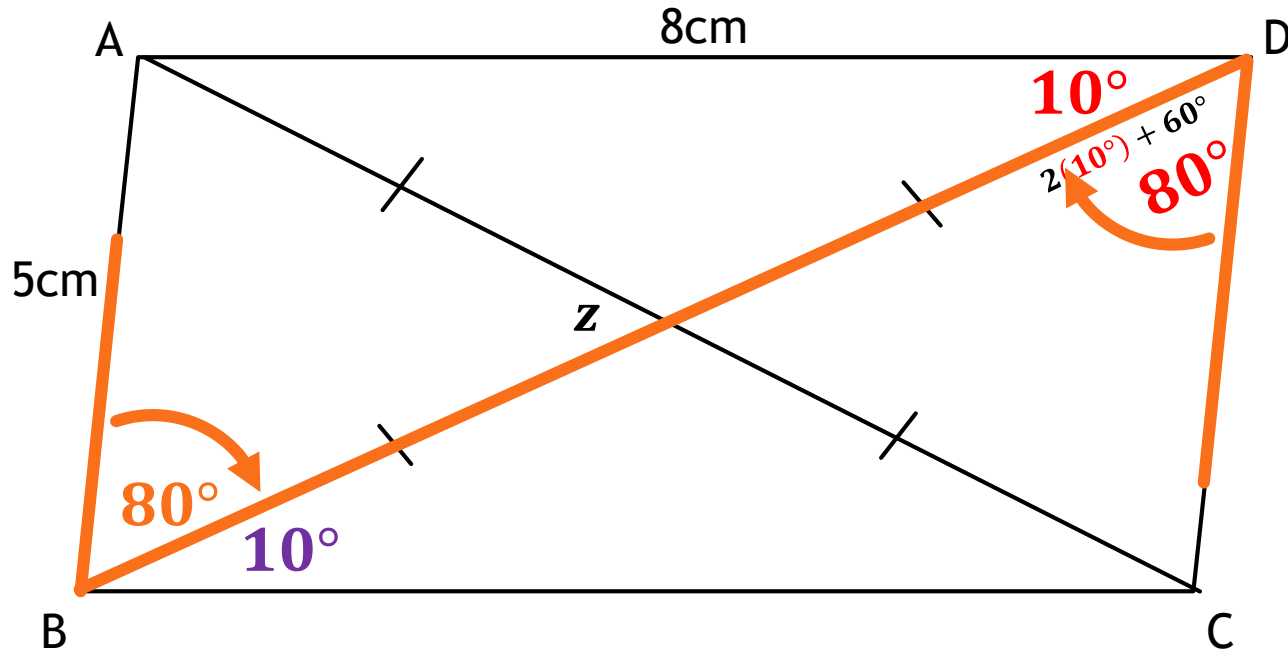
Diagonals are equal (*Square or Rectangle*)
Opposite sides are equal
 \therefore It must be a rectangle

- 2.) Determine giving reasons x , y and z

$$\begin{aligned}x + 2x + 60^\circ &= 90^\circ && \text{Adj Comp } \angle\text{'s or} \\3x &= 90^\circ - 60^\circ && \text{Properties of a rect} \\3x &= 30^\circ \\x &= 10^\circ\end{aligned}$$

$$y = x = 10^\circ \qquad \text{alt } \angle\text{'s } =; AD \parallel BC$$

EXAMPLE:



1.) Classify the quadrilateral ABCD, giving reasons for you answer.

Diagonals are equal (*Square or Rectangle*)
Opposite sides are equal
 \therefore It must be a rectangle

2.) Determine giving reasons x , y and z

$$x + 2x + 60^\circ = 90^\circ \quad \text{Adj Comp } \angle's \text{ or}$$

$$3x = 90^\circ - 60^\circ \quad \text{Properties of a rect}$$

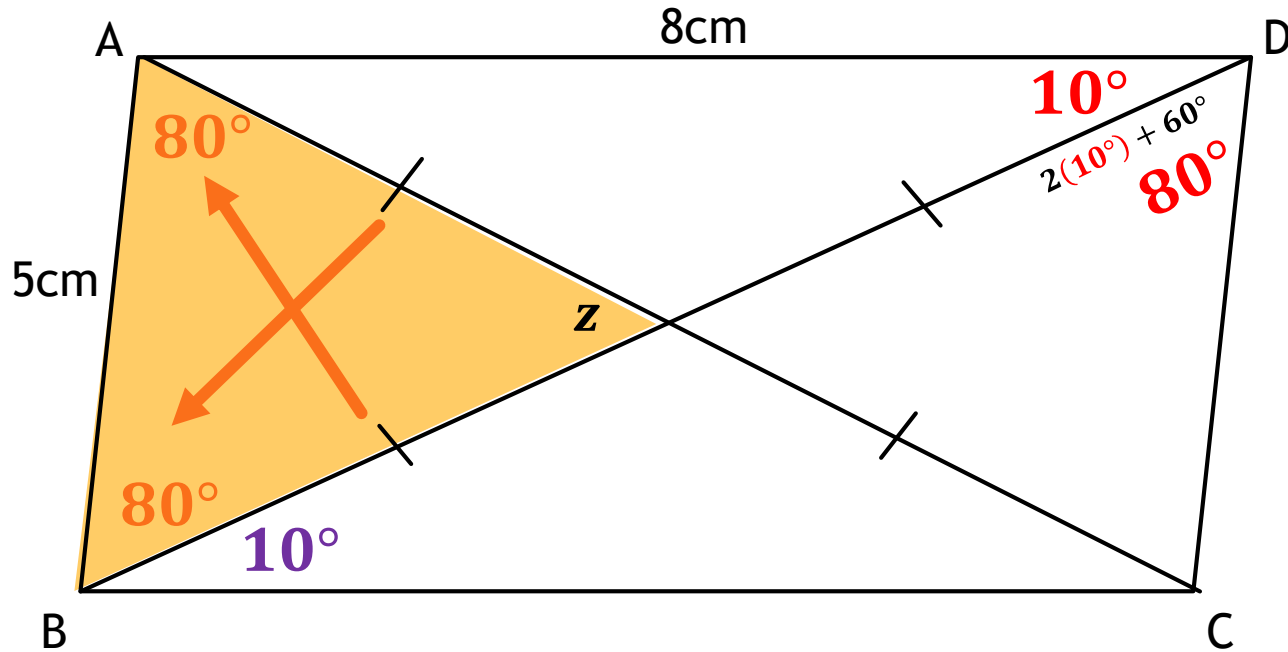
$$3x = 30^\circ$$

$$x = 10^\circ$$

$$y = x = 10^\circ \quad \text{alt } \angle's =; AD \parallel BC$$

$$\widehat{ABD} = 80^\circ \quad \text{alt } \angle's =; AB \parallel DC$$

EXAMPLE:



1.) Classify the quadrilateral ABCD, giving reasons for you answer.

Diagonals are equal (*Square or Rectangle*)
Opposite sides are equal
 \therefore It must be a rectangle

2.) Determine giving reasons x, y and z

$$x + 2x + 60^\circ = 90^\circ \quad \text{Adj Comp } \angle's \text{ or}$$

$$3x = 90^\circ - 60^\circ \quad \text{Properties of a rect}$$

$$3x = 30^\circ$$

$$x = 10^\circ$$

$$y = x = 10^\circ \quad \text{alt } \angle's =; AD \parallel BC$$

$$\hat{A}BD = 80^\circ \quad \text{alt } \angle's =; AB \parallel DC$$

$$\hat{B}AC = 80^\circ \quad \angle's \text{ opp} = \text{sides}$$

$$80^\circ + 80^\circ + z = 180^\circ \quad \angle's \text{ in a } \Delta$$

$$z = 180^\circ - 80^\circ - 80^\circ$$

$$z = 20^\circ$$



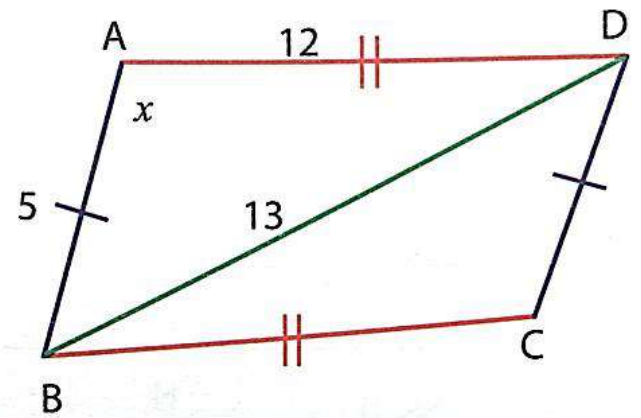
EXERCISE 13.2

Pg. 128 (No. 1,2,3)

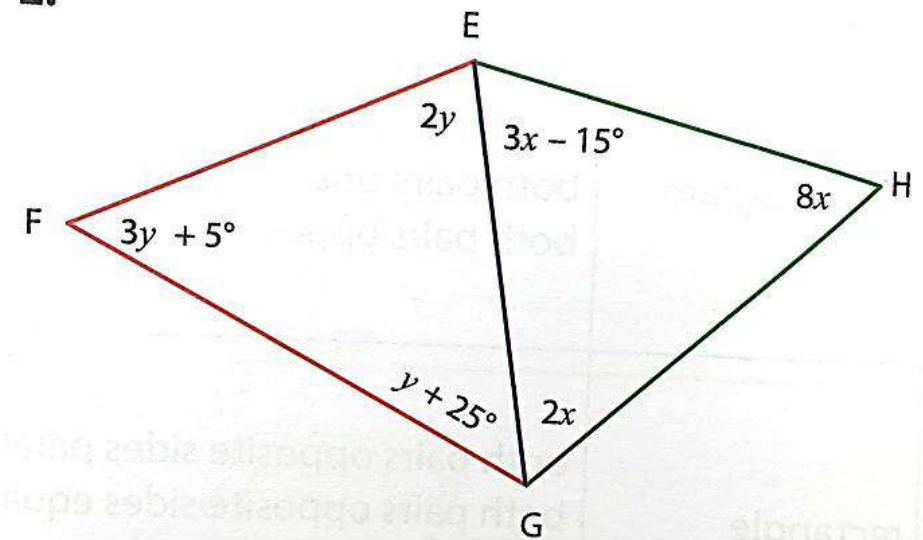
EXERCISE 13.2 Pg. 128 (No. 1,2,3)

Solve for x and/or y where necessary and then classify each quadrilateral. Reasons must be given. Quadrilaterals have not been drawn to scale.

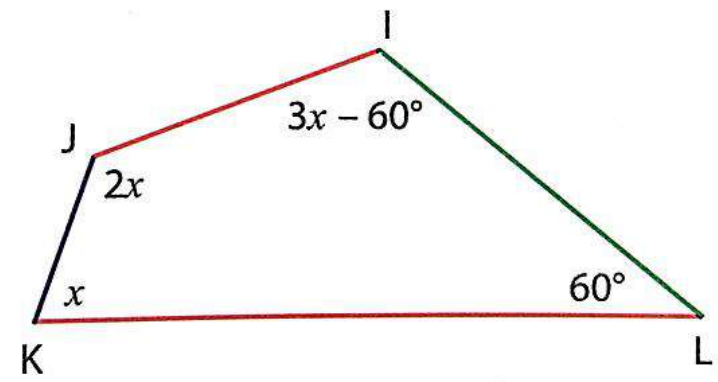
1.



2.



3.



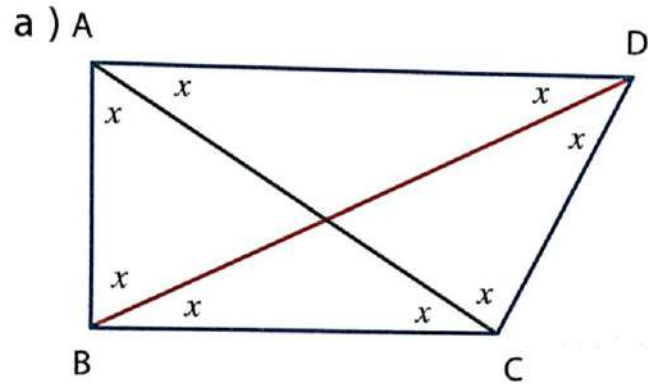


Topic 13

GEOMETRY OF 2D SHAPES VIDEO 3

PROPERTIES OF QUADRILATERALS

Remember these are not drawn to scale!



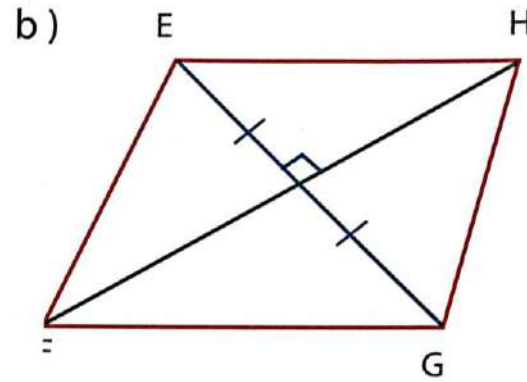
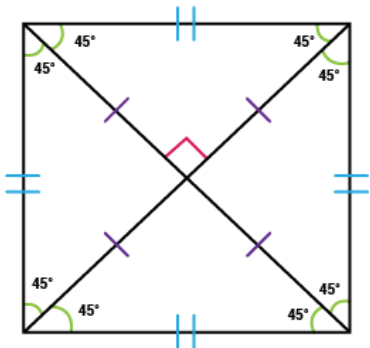
What do we know?

All angles at vertices are bisected
All angles are equal

What can we conclude?

ABCD is a square

What does it look like to scale?



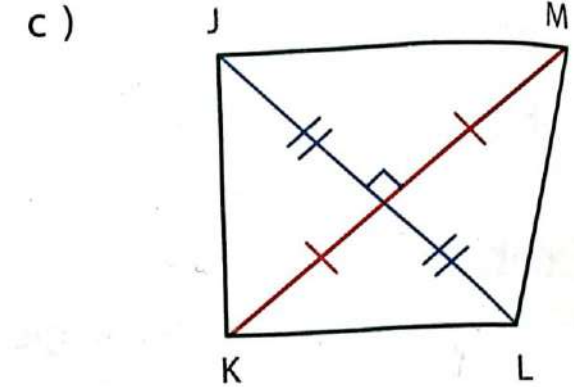
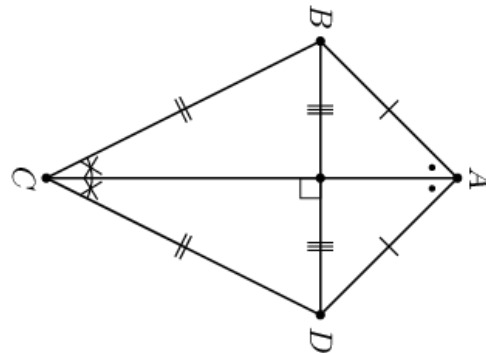
What do we know?

Diagonals intersect at 90°
1 Diagonal is Bisected

What can we conclude?

EFGH is a Kite

What does it look like to scale?



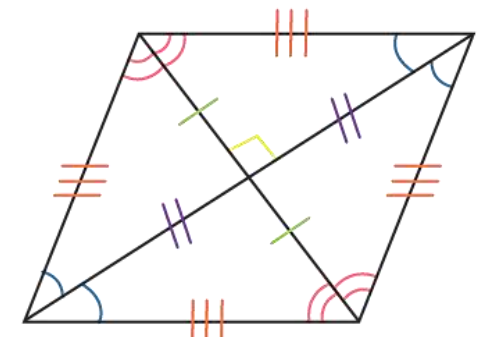
What do we know?

Diagonals intersect at 90°
2 Diagonals are Bisected

What can we conclude?

JKLM is a rhombus

What does it look like to scale?



Properties of Quads Pg.127
Or Sharp Worksheet on
Google Classroom



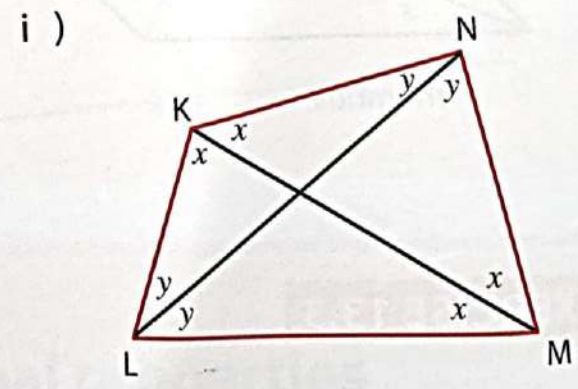
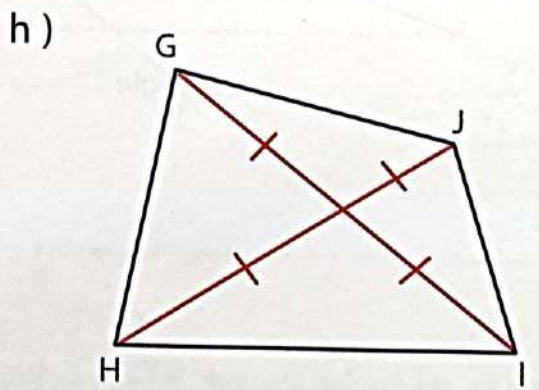
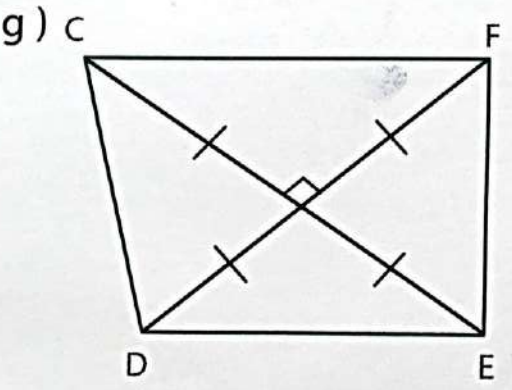
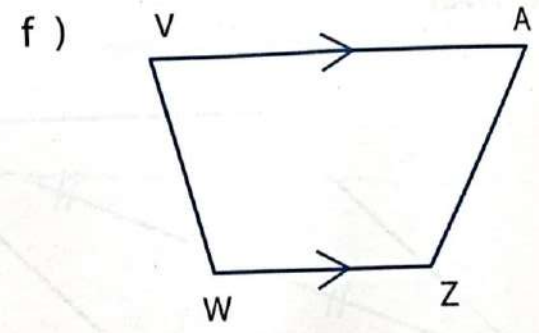
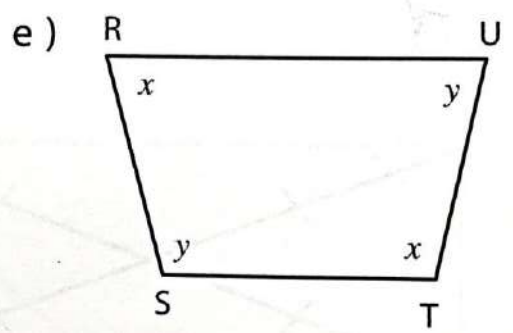
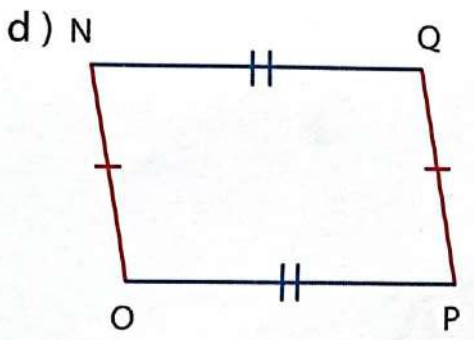
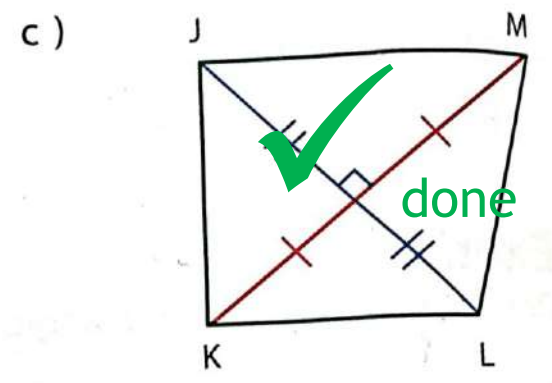
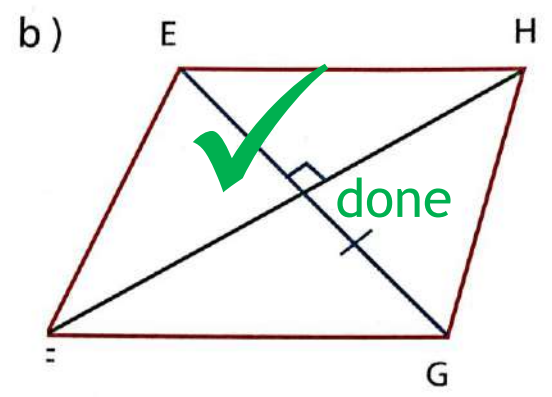
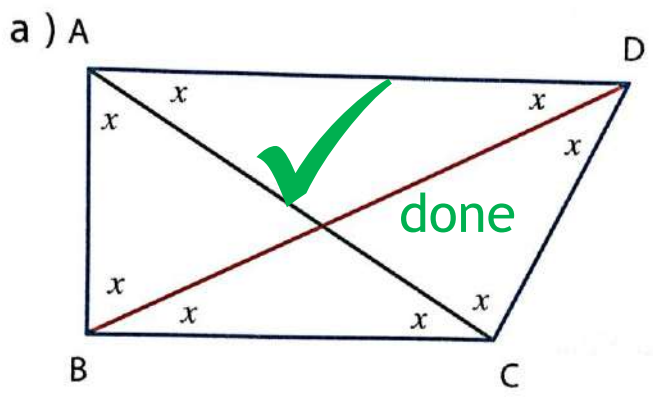
EXERCISE 13.4

Pg. 128 (No. 1d-i)

EXERCISE 13.4 Pg. 130 (No. 1 d,e,f,g,h,i)

Properties of Quads Pg.127
Or Sharp Worksheet on
Google Classroom

Classify each quadrilateral and briefly justify your answer. The sketches are not drawn to scale



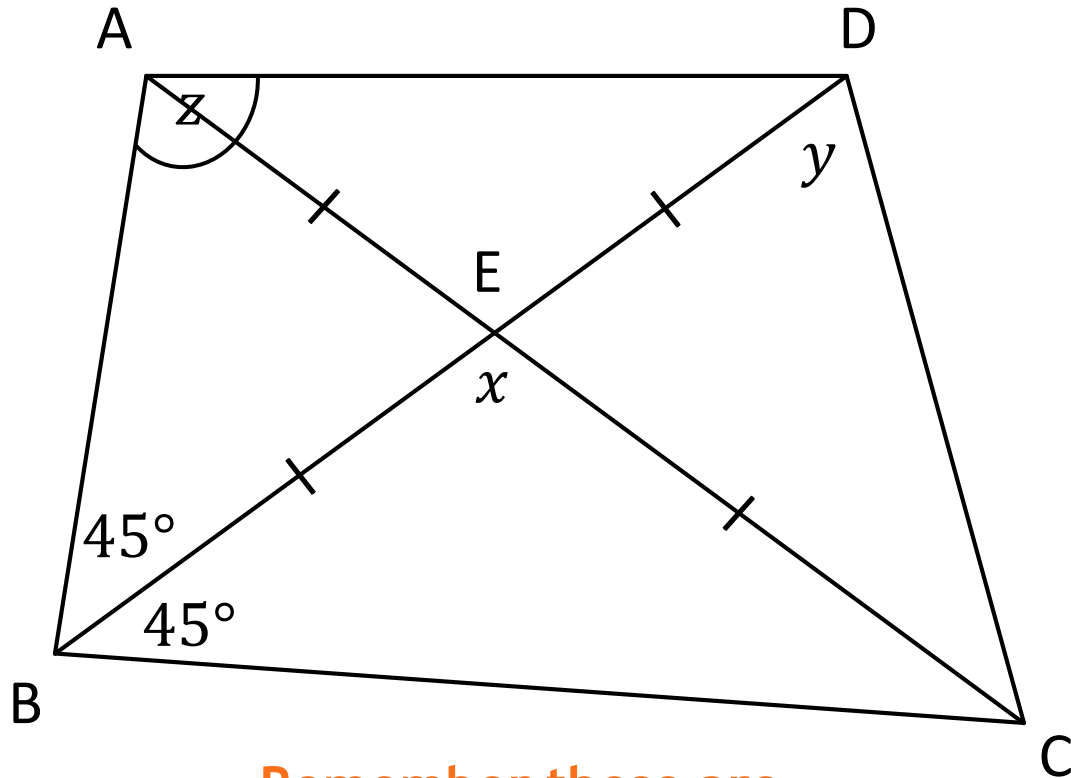


Topic 13

GEOMETRY OF 2D SHAPES VIDEO 4

PROPERTIES OF QUADRILATERALS (Continued)

EXAMPLE:



Remember these are not drawn to scale!

a.) Classify quadrilateral ABCD, giving reasons.

What do we know?

Angles are bisected and equal to 45°

All diagonals are bisected and are equal

What can we conclude?

ABCD is a **square**

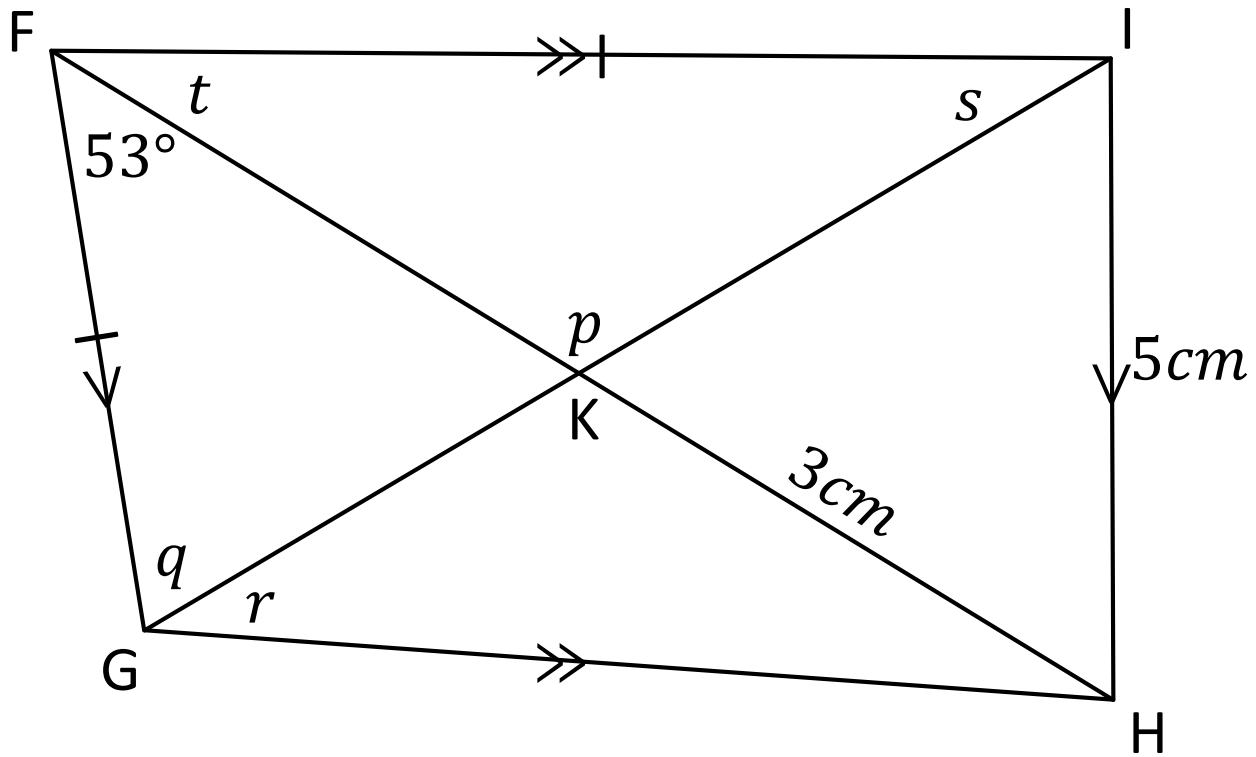
b.) Calculate, giving reasons, x , y and z

| Statement | Reason |
|----------------|--|
| $x = 90^\circ$ | <i>Prop of a square</i> <i>Diagonals intersect at 90°</i> |
| $y = 45^\circ$ | <i>alt \angle's =; $AB \parallel DC$</i> |
| $z = 90^\circ$ | <i>Prop of a square</i> <i>Vertices of a square = 90°</i> |



EXERCISE 13.5

Pg. 131 (No. 2ab)



- Classify quadrilateral $FGHI$, giving reasons.
- Calculate, giving reasons, p, q, r, s and t .