

GRADE 11
Functions 7
Practical problems.

WEBSITE NOTES

TOPIC:

- Practical problems and applications

MAKE SURE YOU GO THROUGH YOUR GRAPH AND FUNCTION NOTES TO HELP YOU.

Example 1

If (2; 7) is the turning point of $f(x) = -2x^2 - 4ax + k$, find the values of the constants a and k .

Answer

Turning point formula for x-coordinate

$$x = \frac{-b}{2a}$$
$$x = \frac{-(-4a)}{2(-2)} = \frac{4a}{-4} = -a$$

Therefore $a = -x$

$x = 2$ (Turning Point)

$a = -2$

Substitute $a = -2$ and $y = 7$ and $x = 2$ into $f(x)$

$$f(x) = -2x^2 - 4ax + k$$

$$7 = -2(2)^2 - 4(-2)(2) + k$$

$$7 = -8 + 16 + k$$

$$7 + 8 - 16 = k$$

$$15 - 16 = k$$

$$-1 = k$$

Therefore $a = -2$ and $k = -1$

Example 2 (Try yourself) -Past Paper Question

QUESTION 5

Given: $f(x) = \frac{4}{x-3} + 2$ and $g(x) = x + 2$

5.1 Write down the equations of the asymptotes of f . (2)

5.2 Determine the x -intercept of f . (3)

5.3 Determine the y -intercept of f . (2)

5.4 Sketch the graphs of f and g on the same system of axes. Show clearly ALL the intercepts with the axes and any asymptotes. (5)

5.5 Calculate the x -coordinates of the points of intersection of f and g . (4)

5.6 If $x < 3$, determine the values of x for which $\frac{4}{x-3} + 2 < x + 2$. (2)

5.7 The line $y = x - 1$ cuts f at P(1 ; 0) and Q. Write down the coordinates of Q. (3)

[21]