

## GRADE 11

### Functions

#### WEBSITE NOTES

##### TOPIC:

- Revise the effect of  $a$  and  $q$  and investigate the effect of  $p$  on the graphs of the functions defined by:
- $y=f(x)=a(x+p)+q$
- $y=f(x)=a(x+p)^2+q$
- $y=f(x)=a(x+p)^2+q$
- $y=f(x)=\frac{a}{x+p}+q$

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## Functions



Characteristics of functions:

- The given  $x$ -value is known as the independent variable, because its value can be chosen freely. The calculated  $y$ -value is known as the dependent variable, because its value depends on the  $x$ -value.
- An asymptote is a straight line, which the graph of a function will approach, but never touch.
- Linear functions of the form  $y = mx + q$ .

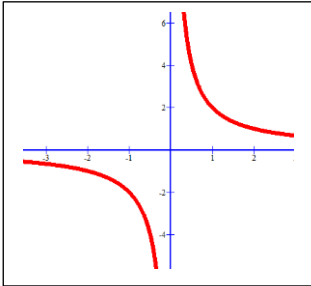
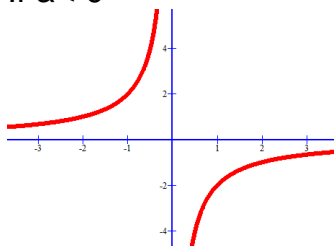
Sketch Graph	Use a table. <b><math>Y=f(x) = x-2</math></b> Substitute the values for $x$ (which you chose) into the equation																								
	<table border="1"><tr><td>X</td><td>-2</td><td>-1</td><td>0</td><td>1</td><td>2</td></tr><tr><td>F(x)</td><td><b>(-2)</b></td><td><b>(-1)</b></td><td>-2</td><td>-1</td><td>0</td></tr><tr><td>=y</td><td>-2</td><td>-2</td><td></td><td></td><td></td></tr><tr><td></td><td>=-4</td><td>=-3</td><td></td><td></td><td></td></tr></table>	X	-2	-1	0	1	2	F(x)	<b>(-2)</b>	<b>(-1)</b>	-2	-1	0	=y	-2	-2					=-4	=-3			
X	-2	-1	0	1	2																				
F(x)	<b>(-2)</b>	<b>(-1)</b>	-2	-1	0																				
=y	-2	-2																							
	=-4	=-3																							
Domain	X E R																								
Range	Y E R																								
$m$ changes	The Slope changes.																								
<b><math>q</math></b> changes	The graph cuts the $y$ axis at $q$ . The graph can shift up or down then in comparison with original graph. Example $f(x) = x-2$ $g(x) = x-5$ The graph of $g(x)$ cuts the $y$ -axis at -5. Therefore $g(x)$ has moved down 3 units from $f(x)$ graph.																								

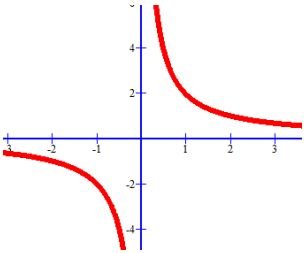
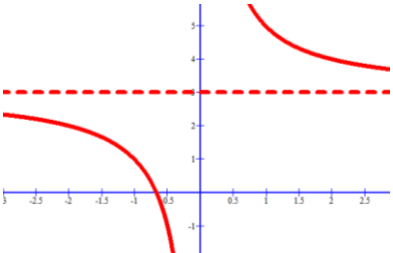
- Parabolic functions of the form  $y = ax^2 + q$ .

Sketch Graph	Use a table. Substitute the values for $x$ (which you chose) into the equation
Domain	X E R

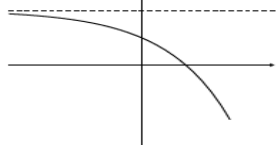
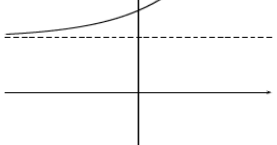
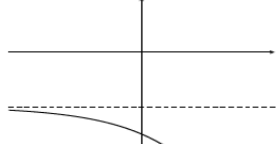
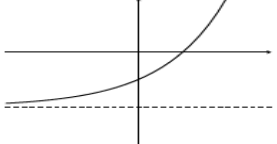
Range	<p><b>If a is positive</b>  <math>Y \geq q</math></p> <p><b>If a is negative</b>  <math>Y \leq q</math></p>
<b>a</b> changes	<p>If <math>a \geq 0</math></p>  <div style="border: 1px solid black; padding: 5px; display: inline-block; margin-left: 20px;">The greater the a value the more narrow the "smile"</div> <p>If <math>a \leq 0</math></p>  <div style="border: 1px solid black; padding: 5px; display: inline-block; margin-left: 20px;">The greater the a value the more narrow the "sad face"</div>
<b>q</b> changes	The graph cuts the y axis at q. The graph can shift up or down then in comparison with original graph.

– Hyperbolic functions of the form  $y = \frac{a}{x} + q$ .

Sketch Graph	Use a table. Substitute the values for x (which you chose) into the equation
Domain	$X \in \mathbb{R}; x \neq 0$
Range	$Y \in \mathbb{R}; y \neq q$
<b>a</b> changes	<p>The value of y at x=1 will be a  The value of y at x = -1 will be a  <b>ALSO REMEMBER</b>  If a &gt; 0</p>  <p>If a &lt; 0</p> 

<p><b>q</b> changes</p>	<p>q indicates the y- asymptote.          If <math>q = 0</math> then the asymptote is <math>y = 0</math> (x-axis)</p>  <p>If <math>q = 3</math> then the asymptote is <math>y = 3</math>, shifting up the graph by 3 units.</p> 

– Exponential functions of the form  $y = ab^x + q$ .

Sketch Graph	Use a table		
Domain	$X \in \mathbb{R}$		
Range	If $a > 0$ $Y \in \mathbb{R}; y < q$ If $a < 0$ $Y \in \mathbb{R}; y < q$		
<p><b>a</b> and <b>b</b> and <b>q</b> changes</p>	$b > 1$	$a < 0$	$a > 0$
	$q > 0$		
	$q < 0$		

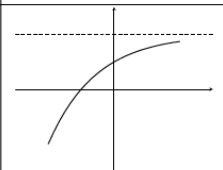
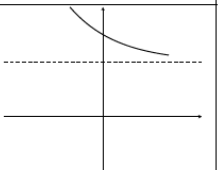
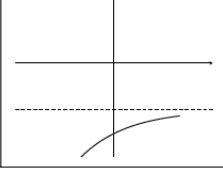
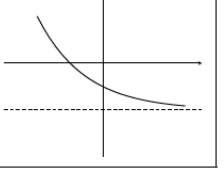
	$0 < b < 1$	$a < 0$	$a > 0$
$q > 0$			
$q < 0$			

Table 6.5: The effect of  $a$  and  $q$  on an exponential graph when  $0 < b < 1$ .

The  $q$  is the Asymptote of the graph. As  $q$  changes the graph will move up or down depending on the value of  $q$ .

<b>Shifts</b>		
For $c > 0$ , to obtain the graph of:		
$f(x)+c$	shift the graph of $f(x)$	upward $c$ units
$f(x)-c$	shift the graph of $f(x)$	downward $c$ units
$f(x+c)$	shift the graph of $f(x)$	left $c$ units
$f(x-c)$	shift the graph of $f(x)$	right $c$ units

<b>Reflections</b>		
To obtain the graph of:		
$-f(x)$	reflect the graph of $f(x)$	about the x-axis
$f(-x)$	reflect the graph of $f(x)$	about the y-axis

<b>Stretches and compressions</b>		
For $c > 1$ , to obtain the graph of:		
$cf(x)$	stretch the graph of $f(x)$	vertically by a factor of $c$
$(1/c)f(x)$	compress the graph of $f(x)$	vertically by a factor of $c$
$f(cx)$	compress the graph of $f(x)$	horizontally by a factor of $c$
$f(x/c)$	stretch the graph of $f(x)$	horizontally by a factor of $c$